Multiple superconducting gap and anisotropic spin fluctuations in iron arsenides: Comparison with nickel analog

Z. Li^a, S. Kawasaki^b, T. Oka^b, T. Tabuchi^b, Y. Ooe^b, M. Ichioka^b, Z. A. Ren^a, Z. X. Zhao^a, J. L. Luo^a, N. L. Wang^a, X. C. Wang^a, Q. Q. Liu^a, C. Q. Jin^a, C.T. Lin^c, Guo-qing Zheng^{a,b}

^aInstitute of Physics and Beijing National Lab for Condensed Matter Physics, Chinese Academy of Science, Beijing, 100190, China ^bDepartment of Physics, Okayama University, Okayama 700-8530, Japan ^cMax Planck Institute, Heisenbergstrasse 1, D-70569 Stuttgart, Germany

The recent discovery of superconductivity in LaFeAsO_{1-x}F_x and the superconductors, while there is no significant electron correlations weaker compared to underdoped copper-oxides or cobalt-oxide superconductivity, iron arsenide, nickel arsenide, NMR

1. Introduction

The recent discovery of superconductivity in LaFeAsO_{1-x}F_x at the transition temperature T_c = 26 K [1] has attracted great attention. Soon after the initial work, T_x was raised to 55 K in Smr&AsO_{1-x}F_x [2], which is the highest among materials except currentes. These compounds have a ZrCuSiAs type structure. By placing Ba with K, holes are doped and T_c can be as high as 38 K [3]. Another arsenide, LiFeAs Go-called 1112 compound, several other personal structure, was discovered to swo superconductivity even in stoichiometric composition[4]. The common feature of these three systems are the iron arsenide plane which dominates the properties of these compounds and the monitoring of these compounds and the feature of these three systems are the iron arsenide plane which dominates the properties of these compounds and the feature of these three systems are the iron arsenide plane which dominates the properties of these compounds and the feature of these three systems are the iron arsenide plane which dominates the properties of these compounds and the feature of these three systems are the iron arsenide plane which dominates the properties of these compounds and the feature of these three systems are the iron arsenide plane which dominates the properties of these compounds and the feature of these three systems are the iron arsenide plane which dominates the properties of these compounds and the feature of these compounds and the feature of these three systems are the iron arsenide plane which dominates the properties of these compounds and the feature of these three systems are the iron arsenide plane which dominates the properties of these compounds and the feature of the surface of these compounds and the feature of the feature of the plane which dominates the properties of these compounds and hosts the superconductivity.

We have used nuclear magnetic resonance (NMR) and nuclear quadrupole resonance (NQR) techniques to study the pairing symmetry and spin fluctuations in the normal state. We find that these supercondutors are in the spin-singlet state with multiple gaps, and the latter property is quite different from the cuprate case. The antiferromagnetic spin fluctuation is weaker than the cuprates and are anisotropic in the spin space.

creases below T_c , as seen in Fig. 2. The behavior is quite similar to the PrFeAs_{0.89}F_{0.11} case. These results indicate spinsinglet superconductivity.

However, the detailed T variation of the Knight shift is different from that seen in usual spin-singlet superconductors such as copper-oxides, where K decreases rapidly below T_c which is followed by a milder decrease at low temperatures, as illustrated by the broken curve in Fig. 1. In contrast, the decrease of the Knight shift shows a step-wise behavior at a temperature about half the T_c .

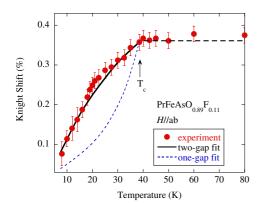


Figure 1: (color online) The temperature variation of 75 As Knight shift of PrFeAs_{0.89}F_{0.11} with $H \parallel ab$. The solid curve is a fitting of two d-wave gaps with $\Delta_1(T=0)=3.5k_BT_C$ and a relative weight of 0.4, and $\Delta_2(T=0)=1.1k_BT_C$ with a relative weight of 0.6 (see text). The broken curve below T_c is a simulation for the larger gap alone.

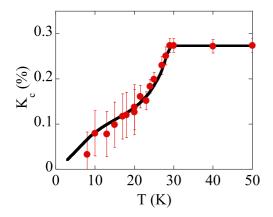


Figure 2: (color online) The Knight shift data of $Ba_{0.72}K_{0.28}Fe_2As_2$ with $H \parallel c$ -axis. The arrow indicates T_c . The curve below T_c is a fit to a two-gap model (see text).

3.2. T_1 in the superconducting state

The step-wise decrease of the Knight shift is also reflected in the temperature dependence of the $^{19}\mathrm{F}$ spin-lattice relaxation rate $1/T_1$ [9], and is also seen in LaFeAsO_{0.92}F_{0.08} (T_c =23 K)[11] and the hole-doped Ba_{0.72}K_{0.28}Fe₂As₂ (T_c =31.5 K)[10]. Figure 3 shows the temperature dependence of $1/T_1$ measured by $^{19}\mathrm{F}$ NMR in PrFeAs_{0.89}F_{0.11} (T_c =45 K), and Fig. 4 shows the temperature dependence of $1/T_1$ measured by $^{75}\mathrm{As}$ NQR in LaFeAsO_{0.92}F_{0.08} (T_c =23 K). Below T_c , there is no coherence peak for both samples. Moreover, a bending feature is seen around $T\sim T_c/2$ [9, 11]. This behavior is not expected in a single-gap superconductor.

Figure 5 shows the temperature dependence of $1/T_1$ measured by ⁷⁵As NMR with the magnetic field applied along the c-axis in Ba_{0.72}K_{0.28}Fe₂As₂ ($T_c = 31.5$ K) single crystal [10]. $1/T_1$ also shows a "knee"-shape around $T \sim T_c/2$. Namely, the sharp drop of $1/T_1$ just below T_c is gradually replaced by a slower change below $T \sim 15$ K, then followed by another steeper drop below. This "convex" shape is clearly different from the case of superconductors with a single gap which shows

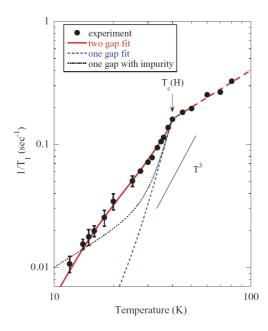


Figure 3: (color online) The temperature dependence of 19 F spin-lattice relaxation rate $1/T_1$ in PrFeAs_{0.89}F_{0.11} measured at $\mu_0 H = 1.375$ T. The broken line indicates a relation of $T_1 T$ =const which holds for a weakly correlated electron system. The thin straight line illustrates the temperature dependence of T^3

a "concave" shape of *T*-variation.

We find that a two-gap model can reproduce the step-wise T variation of $1/T_1$ and the Knight shift. The underlying physics is that the system is dominantly governed by a larger gap for T near T_c while at sufficiently low T it starts to "notice" the existence of a smaller gap, resulting in another drop in $1/T_1$ below $T \sim T_c/2$. In the d-wave case with two gaps, where the density of states (DOS) is $N_{s,i}(E) = N_{0,i} \frac{E}{\sqrt{E^2 - \Delta_i^2}}$, the Knight shift and $1/T_{1s}$ in the superconducting state are written as

$$\frac{K_s}{K_N} = \int N_s(E) \frac{\partial f(E)}{\partial E} dE \tag{1}$$

$$\frac{T_{1N}}{T_{1s}} = \sum \frac{2}{k_B T} \int \int N_{s,i}(E) N_{s,i}(E')$$

$$f(E)\left[1 - f(E')\right]\delta(E - E')dEdE' \tag{2}$$

where f(E) is the Fermi distribution function. We find that the parameters $2\Delta_1(0) = 7.0k_BT_c$, $2\Delta_2(0) = 2.2k_BT_c$ and $\kappa = 0.4$ can fit the data of both the shift and $1/T_1$ very well, as shown by the solid curves in Fig. 1 and Fig. 3, where

$$\kappa = \frac{N_{0,1}}{N_{0,1} + N_{0,2}} \tag{3}$$

is the relative DOS of the band(s) with larger gap to the total DOS.

Application of the same model to LaFeAsO_{0.92}F_{0.08} gives $2\Delta_1(0) = 8.4k_BT_c$, $2\Delta_2(0) = 3.2k_BT_c$, and $\kappa = 0.6$ [11]. On the other hand, for Ba_{0.72}K_{0.28}Fe₂As₂, $2\Delta_1(0) = 9.0 k_BT_c$, $2\Delta_2(0) = 1.62k_BT_c$, and $\kappa = 0.69$ was obtained [10]. The same model can also fit the Knight shift data, as seen in Fig. 2.

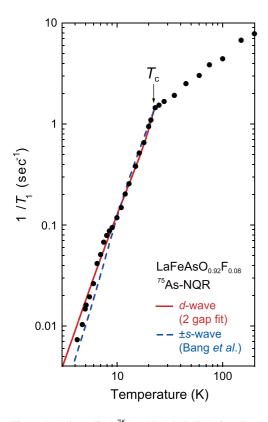


Figure 4: (color online) ⁷⁵As $(1/T_1)$ in LaFeAsO_{0.92}F_{0.08}. The solid curve is a two gap fit assuming a d-wave symmetry with parameters, $\Delta_1(0)=4.2k_BT_c$, $\Delta_2(0)=1.6k_BT_c$, and $\kappa=0.6$ (see text). The dotted curve is a simulation assuming two s-wave gaps that change signs with parameters, $\Delta_1(0)=3.75k_BT_c$, $\Delta_2(0)=1.5k_BT_c$, and $\kappa=0.38$.

For the case of s^{\pm} -gap [12, 13], recent calculations have shown that scattering between the different bands may reduce the coherence peak just below T_c [14, 15]. Following Ref.[15], we calculated $1/T_1$ for the s^{\pm} -gap model, by introducing the impurity scattering parameter η in the energy spectrum, $E = \omega + i\eta$. The parameters $2\Delta_1(0) = 7.5k_BT_c$, $2\Delta_2(0) = 3.0k_BT_c$, $\kappa = 0.38$ and $\eta = 0.15k_BT_c$, can well fit the data, as shown in Fig. 4. where

$$\eta = \frac{\pi n_{\text{imp}}(N_1 + N_2)V^2}{1 + \pi^2(N_1 + N_2)^2 V^2} \tag{4}$$

In the equation, $n_{\rm imp}$ is the impurity concentration and V is the scattering potential at the impurity. A similar set of parameters $(2\Delta_1(0) = 7.2k_{\rm B}T_{\rm c}, 2\Delta_2(0) = 1.68k_{\rm B}T_{\rm c}, \kappa = 0.6$ and η =0.22 $k_{\rm B}T_{\rm c}$) can fit the data of Ba_{0.72}K_{0.28}Fe₂As₂, see Fig. 5.

The results for LiFeAs[16] (Fig. 6) are shown in Fig. 6. We measured two Li_xFeAs samples with nominal x=0.8 and 1.1. The physical properties including the NMR results are the same. This supports that only stoichiometric compound can be formed.[17] $1/T_1$ below T_c shows a qualitatively similar behavior as the previous three samples, but the behavior at low temperatures is a little different. Namely, $1/T_1$ becomes to be proportional to T below $T \le T_c/4$, which indicates that a finite DOS is induced by the impurity scattering. Obviously, this would occur in a d-wave case. On the other hand, it is also possible in the s^{\pm} case provided that the scattering between the electron- and hole-pocket is strong. Calculation by the s^{\pm} -

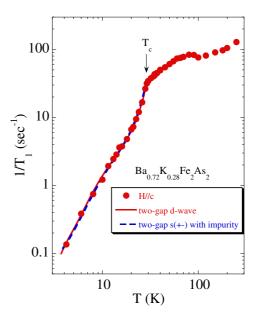


Figure 5: (color online) T-dependence of $1/T_1$ in $Ba_{0.72}K_{0.28}Fe_2As_2$. The curves below T_c (indicated by the arrow) are fits to two-gap models (see text).

wave model shows that the gap value of LiFeAs is smaller than other compounds, but the impurity scattering is much larger $(\eta = 0.26k_BT_c)$ [16]. The gap parameters for all Fe-arsenide samples are summarized in Tab. 1. To summarize, the multiple gap feature is universal to all Fe-arsenids, which probably associated with the multiple electronic bands [18].

By strong contrast, the nickel analog of LaFeAsO_{1-x} F_x , namely, LaNiAsO_{0.9}F_{0.1} has different behavior.[19] As seen in Fig. 7, $1/T_1$ shows a well-defined coherence peak just below T_c , which is a finger print of superconductors with an isotropic gap. This is in sharp contrast to various Fe-arsenides reported so far[9, 11, 10, 20, 21, 22]. At low temperatures, $1/T_1$ decreases as an exponential function of T. The solid curves in Fig. 7 are calculations using the BCS model. Following Hebel [23], we convolute $N_s(E)$ with a broadening function B(E) which is approximated with a rectangular function centered at E with a height of $1/2\delta$. The solid curves below T_c shown in Fig. 7 is calculation with $2\Delta(0) = 3.2k_BT_c$ and $r \equiv \Delta(0)/\delta=5$. Such Tdependence of $1/T_1$ in the superconducting state is in striking contrast to that for Fe-arsenide where no coherence peak was observed and the T-dependence at low-T does not show an exponential behavior. The striking difference may be ascribed to the different topology of the Fermi surfaces. For Fe-arsenides, it has been proposed that d-wave [24, 25] or sign reversal s-wave gap [12, 13] can be stabilized due to nesting by the connecting wave vector $Q = (\pi, 0)$. In LaNiAsO_{0.9}F_{0.1}, however, there is no such Fermi surface nesting [26], and thus the mechanism for the proposed gap symmetry does not exist. Given that the T_c is much lower in LaNiAs $O_{1-x}F_x$, our result suggests the important role of the Fermi-surface topology in the superconductivity

Finally, for comparison, $1/T_1$ normalized by the value at T_c are shown in Fig. 8 as a function of reduced temperature for all

Table 1: The gap parameters. $\kappa = N_1/(N_1 + N_2)$, $\eta = \frac{\pi n_{\text{imp}}(N_1 + N_2)V^2}{1 + \pi^2(N_1 + N_2)^2V^2}$, where n_{imp} is the impurity concentration and V is the scattering potential at the impurity.

	d-wave			s [±] -wave			
	$\Delta_1/k_{\rm B}T_c$	$\Delta_2/k_{\rm B}T_c$	К	$\Delta_1/k_{\rm B}T_c$	$\Delta_2/k_{ m B}T_c$	K	$\eta/k_{\mathrm{B}}T_{c}$
PrFeAsO _{0.89} F _{0.11}	3.5	1.1	0.4				
$LaFeAsO_{0.92}F_{0.08}$	4.2	1.6	0.6	3.75	1.5	0.38	0.15
$Ba_{0.72}K_{0.28}Fe_2As_2$	4.5	0.81	0.69	3.6	0.84	0.6	0.22
LiFeAs				3.0	1.3	0.5	0.26

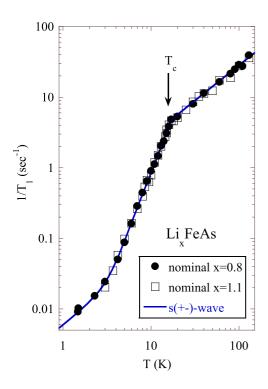


Figure 6: (color online) The T-dependence of $1/T_1$ measured by NQR for Li_{0.8}FeAs and Li_{1.1}FeAs. The curves below $T_{\rm c}$ are fits to the s^\pm -wave model with $\Delta_1^+=3.0~k_{\rm B}T_{\rm c},$ $\Delta_2^-=1.3~k_{\rm B}T_{\rm c},$ and the impurity scattering rate $\eta=0.26~k_{\rm B}T_{\rm c}$ (see text).

samples.

3.3. Normal state properties

Next, we discuss on the character of spin fluctuations. Figure 9 shows the temperature variation of $1/T_1T$ in $Ba_{0.72}K_{0.28}Fe_2As_2$. One notices that, in the normal state above T_c , $1/T_1T$ increases with decreasing T, which is an indication of antiferromagnetic electron correlation, since both K^a and K^c slightly decrease with decreasing T, but becomes a constant below $T \sim 70$ K [10], which resembles closely the cuprate [27] or cobaltate cases [28].

Figure 10 compares $1/T_1T$ for four samples. The data for LaFeAsO_{0.92}F_{0.08}, LiFeAs, LaNiAsO_{0.9}F_{0.1} are measured by NQR, which correspond to $H \parallel c$ -axis, since the principle axis of the NQR tensors is along the c-axis. The data for Ba_{0.72}K_{0.28}Fe₂As₂ is measured by NMR with $H \parallel c$ -axis. The $1/T_1T$ of hole-doped Ba_{0.72}K_{0.28}Fe₂As₂ increase with decreasing temperature as discussed above. The electron-doped LaFeAsO_{0.92}F_{0.08} also show similar behavior, although

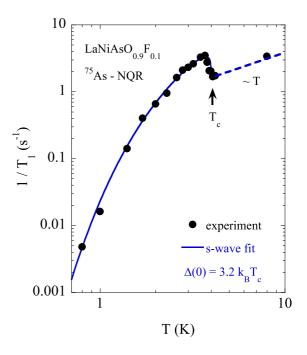


Figure 7: (color online) The T dependence of the spin lattice relaxation rate, $1/T_1$, for LaNiAsO_{0.9}F_{0.1}. The arrows indicate T_c . The broken straight lines show the relation $1/T_1 \propto T$, and the curves below T_c are fits to the BCS model with the gap size indicated in the figure.

the increasing is very small. The $1/T_1T$ of stoichiometric LiFeAs is almost constant. While $1/T_1T$ of LaNiAsO_{0.9}F_{0.1} decrease with decreasing temperature. These results suggest that the antiferromagnetic spin fluctuations are stronger in Ba_{0.72}K_{0.28}Fe₂As₂ and LaFeAsO_{0.92}F_{0.08}, but quite weak in LiFeAs and LaNiAsO_{0.9}F_{0.1}. This difference may be understood by the difference of the Fermi surface topology. There are not only hole-pockets and electron-pockets but also nesting between them in Ba_{0.72}K_{0.28}Fe₂As₂ and LaFeAsO_{0.92}F_{0.08}, which can promote spin fluctuations. While in LiFeAs there is no such nesting, although there are still hole-pockets and electron-pockets. Lacking of such nesting make the spin fluctuation become weaker than Ba_{0.72}K_{0.28}Fe₂As₂ and LaFeAsO_{0.92}F_{0.08}. In LaNiAsO_{0.9}F_{0.1} there is no hole-pockets, then nesting can not happen, therefore the spin fluctuations are not expected.

Finally, we discuss the anisotropy of the spin fluctuations. In a general form, $1/T_1T$ is written as

$$\frac{1}{T_1 T} = \frac{\pi k_B \gamma_n^2}{(\gamma_e \hbar)^2} \sum_q A_{hf}^2 \frac{\chi_\perp''(q, \omega)}{\omega},\tag{5}$$

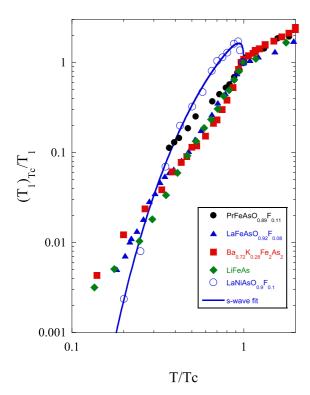


Figure 8: (color online) The normalized T-dependence of $1/T_1$ for $PrFeAs_{0.89}F_{0.11}$ (T_c =45 K), $LaFeAsO_{0.92}F_{0.08}$ (T_c =23 K), $Ba_{0.72}K_{0.28}Fe_2As_2$ $(T_c = 31.5 \text{ K})$. LiFeAs $(T_c = 17 \text{ K})$, LaNiAsO_{0.9}F_{0.1} $(T_c = 4.0 \text{ K})$.

where $\chi''_{\perp}(q,\omega)$ is the imaginary part of the dynamical susceptibility perpendicular to the applied field. The anisotropic ratio in the form of $\frac{\sum_{\bf q} A_{hf}^c({\bf q})^2 \chi_c''({\bf q})}{\sum_{\bf q} A_{hf}^a({\bf q})^2 \chi_d''({\bf q})}$ for $Ba_{0.72}K_{0.28}Fe_2As_2$ and parent compound are shown in Fig.11. The larger magnitude of $1/T_1T$ along the a-axis direction than that along the c-axis direction indicates that there are stronger fluctuations along the c-axis direction seen by the As-site. Neutron experiment found that, in the undoped BaFe₂As₂ compound, the ordered Fe magnetic moment is along the a-direction and forms a stripe [29]. Since the As atom sits in the position above (below) the middle of four Fe-atoms, our result implies that, in the Fe site, a stronger fluctuating fields exist along the a-axis direction, as illustrated in the inset of Fig. 9. It is remarkable that the antiferromagnetic fluctuations of Fe are anisotropic in spin space. Namely, $\chi''_{\pm}(Q)$ is much larger than $\chi''_{zz}(Q)$, where z is along the c-axis direction and Q is the spin fluctuation wave vector. This is in contrast to the high- T_c cuprates where the spin fluctuations are believed to be isotropic, but similar situation was encountered in cobaltate superconductor [30]. The relationship between the energyand q-dependence of the spin fluctuations (SF) and possible SFinduced superconductivity has been studied both theoretically [31] and experimentally [32]. To our knowledge, however, the relationship between the anisotropy of SF and superconductivity has been less explored so far. We hope that our results will stimulate more theoretical work in this regard.

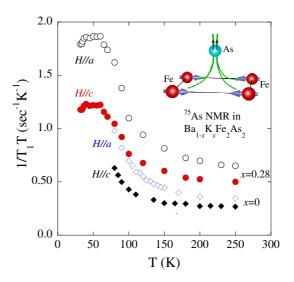


Figure 9: (color online) The quantity $^{75}(1/T_1T)$ in the normal state of Ba_{0.72}K_{0.28}Fe₂As₂ (circles) and in the paramagnetic state of BaFe₂As₂ (diamonds). The arrows in the inset illustrate the larger component of the fluctuating field of Fe and that seen by the As site.

4. Conclusion

In summary, we have presented the NMR and NQR results on the electron-doped Fe-arsenides PrFeAs_{0.89}F_{0.11} ($T_c = 45$ K), LaFeAsO_{0.92}F_{0.08} ($T_c = 23$ K), stoichiometric LiFeAs(T_c = 17 K), and the hole-doped Fe-arsenide $Ba_{0.72}K_{0.28}Fe_2As_2$ (T_c = 31.5 K). We find there are multiple gaps in iron arsenides where Knight shift and $1/T_1$ does not follow a simple powerlaw nor exponential function. However, the $1/T_1$ of the Nickel analog LaNiAsO_{0.9}F_{0.1} shows a well-defined coherence peak just below T_c and an exponential behavior at lower temperatures. These properties indicate that it is a conventional BCS superconductor. The difference between the Fe-arsenides and the Ni-analog may be understood by the differene of the Fermi surface topology, and therefore highlights the important role of the Fermi-surface topology in pairing symmetry of the iron arsenides superconductors.

In the normal state, all iron arsenides show weak antiferromagnetic spin correlations. Our data also show that the sample with weaker correlations has a lower T_c , and this may imply the T_c has a relationship with the structure of Fermi surface. Moreover, the spin fluctuations are anisotropic in spin space, which is different from cuprates.

We gratefully acknowledge the support from CAS, National Science Foundation of China, JSPS and MEXT of Japan.

References

- [1] Y. Kamihara et al, J. Am. Chem. Soc. 130, 3296 (2008).
- Z. -A. Ren et al, Chin. Phys. Lett. 25, 2215 (2008).
- [3] M. Rotter et al. Phys. Rev. Lett. 101, 107006 (2008).
- X. C. Wang et al, Solid State Commun. 148, 538 (2008).
- Z.-A. Ren et al, Materials Research Innovations 12, 105 (2008).
- [6] G. F. Chen et al, Phys. Rev. Lett. 101, 057007 (2008). Z. Li et al, Phys. Rev. B 78, 060504(R) (2008).
- [8] G.L. Sun et al, arXiv:0901.2728 (2009).

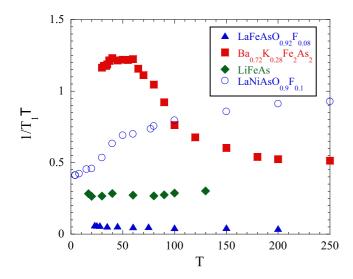


Figure 10: (color online) The T-dependence of $1/T_1T$ for LaFeAsO $_{0.92}$ F $_{0.08}$ (T_c =23 K),Ba $_{0.72}$ K $_{0.28}$ Fe $_2$ As $_2$ (T_c =31.5 K), LiFeAs(T_c =17 K), LaNiAsO $_{0.9}$ F $_{0.1}$ (T_c =4.0 K).

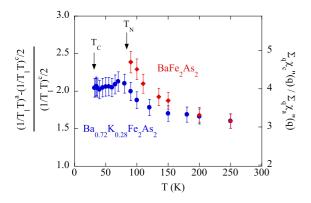


Figure 11: (color online) The T dependence of the anisotropy of the spin fluctuations seen at the As site in terms of $\frac{\sum_{\bf q} A_{hf}^{c}({\bf q})^{2}\chi_{c}^{c'}({\bf q})}{\sum_{\bf q} A_{hf}^{a}({\bf q})^{2}\chi_{d}^{c'}({\bf q})}$ for the left axis and $\frac{\sum_{\bf q} \chi_{c}^{c'}({\bf q})}{\sum_{\bf q} \chi_{d}^{c'}({\bf q})}$ for the right axis.

- [9] K. Matano et al, Europhys. Lett. 83, 57001 (2008).
- [10] K. Matano et al, Europhys. Lett. 87, 27012 (2009).
- [11] S. Kawasaki et al, Phys. Rev. B 78, 220506 (R) (2008).
- [12] I. I. Mazin et al, Phys. Rev. Lett. 101, 057003 (2008).
- [13] K. Kuroki et al, Phys. Rev. Lett. 101, 087004 (2008).
- [14] A.V. Chubukov et al, Phys. Rev. B 78, 134512 (2008). D. Parker et al, ibid, 134524 (2008). M. M. Parish et al, ibid, 144514 (2008).
- [15] Y. Bang and H.-Y. Choi, Phys. Rev. B 78, 134523 (2008); Y. Nagai et al, New J. Phys. 10, 103026 (2008).
- [16] Z. Li et al J. Phys. Soc. Jpn. 79, 083702 (2010).
- [17] X. C. Wang et al, Solid State Commun. 148, 538 (2008) J. H. Tapp et al, Phys. Rev. B 78, 060505 (2008).
- [18] D.J. Singh and M. H. Du, Phys. Rev. Lett. 100, 237003 (2008).
- [19] T. Tabuchi et al, Phys. Rev. B 81, 140509 (2010).
- [20] Y. Nakai et al, J. Phys. Soc. Jpn. 77, 073701 (2008).
- [21] H.-J. Grafe et al, Phys. Rev. Lett. 101, 047003 (2008).
- [22] H. Fukazawa et al, J. Phys. Soc. Jpn. 78, 033704 (2009).
- [23] L. C. Hebel, Phys. Rev. 116, 79 (1959).
- [24] S. Graser et al, New J. Phys. 11, 025016 (2009).
- [25] K. Kuroki et al, Phys. Rev. B 79, 224511 (2009).
- [26] G. Xu *et al*, Europhys. Lett, **82**, 67002 (2008) .
- [27] G.-q. Zheng et al, Phys. Rev. Lett. 90, 197005 (2003).
- [28] G. q. Zheng et al, Phys. Rev. B 73, 180503 (R) (2006).
- [29] Q. Huang et al, , Phys. Rev. Lett. 101, 257003 (2008)

- [30] K. Matano et al, Europhys. Lett. 84, 57010 (2008).
- [31] T. Moriya and K. Ueda, J. Phys. Soc. Jpn. 63, 1871 (1994); D. Monthoux and D. Pines, Phys. Rev. B 49, 4261 (1994).
- [32] G.-q. Zheng et al, J. Phys. Soc. Jpn. 64, 3184 (1995).